

h(x) FUNCTION Summary TEMPLATE

Introduction

$$f(x) \rightarrow f(Bx) \rightarrow f(Bx + C) \rightarrow Af(Bx + C) \rightarrow Af(Bx + C) + D = h(x)$$

$$\left[\begin{array}{c} \text{MATH by Wilson} \\ \text{Your Personal Mathematics Trainer} \\ \text{MathByWilson.com} \end{array} \right]$$

Given a basic function $f(x)$, we know its properties and graph. With the parameters A , B , C , & D shown above, we can start with this basic function $f(x)$ and stretch/contract, translate, and reflect its graph horizontally and vertically to obtain a new function $h(x)$. The attachment provides specific details on how the four (4) parameters affect the graph of $f(x)$, but first we need to know the order in which to apply these parameters. After the graph of $h(x)$ is obtained, it is easy to determine its properties.

We consider “ x ” first since it represents the domain: $Bx + C$. Since multiplication is preformed before addition, the parameter “ B ” comes first in the process:

$$f(x) \rightarrow f(Bx)$$

The “ B ” parameter stretches or contracts the graph of $f(x)$ horizontally and if $B < 0$, it also reflects it with respect to the y -axis.

Next, the parameter “ C ” translates the graph of $f(Bx)$ horizontally:

$$f(Bx) \rightarrow f(Bx + C)$$

Since $A f(Bx + C) + D = A y + D$ deals with y values, next is the parameter “ A ” since multiplication precedes addition.:

$$f(Bx + C) \rightarrow A f(Bx + C)$$

The “ A ” parameter stretches or contracts the graph of $f(Bx + C)$ vertically and also reflects it in the x -axis if $A < 0$.

Finally, the parameter “ D ” translates the graph of $A f(Bx + C)$ vertically:

$$A f(Bx + C) \rightarrow A f(Bx + C) + D = h(x)$$

Again, refer to the attached template for specific details on how to apply the four (4) parameters.