

Inequalities Quadratic

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Recall that we can solve *linear inequalities* by finding the solution of the corresponding equation (called a **Boundary Point**) and testing the two (2) regions it defines by selecting any point in each region and seeing if the original inequality is true (or false). This is called a **Test Point Method** and will be modified to solve quadratic Inequalities:

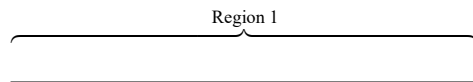
Procedure (Test Point Method):

1. With the quadratic inequality in standard form

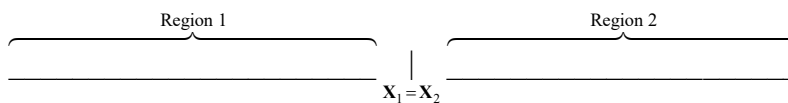
$$ax^2 + bx + c \left\{ \begin{array}{l} < \\ \leq \\ > \\ \geq \end{array} \right\} 0$$

find the solutions $x_1 ; x_2$ of $ax^2 + bx + c = 0$. The solutions divide the horizontal number line into regions:

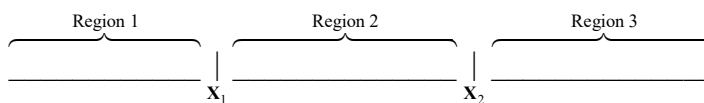
- a. One (1) region if the solutions are complex numbers.**



- b. Two (2) regions if the solutions are the same real number, that is $x_1 = x_2$.**



- c. Three (3) regions if the solutions differ, that is, $x_1 \neq x_2$**



3	$(x - 6)(x + 4) \geq 0$	
4	Determine Boundary Points: $(x + 4)(x - 6) = 0$ $x = -4 ; x = 6$	
5	Check Boundary Points: 1. $x = -4 : ([-4] - 3)([-4] + 1) \stackrel{?}{\geq} 21$ $(-7)(-3) \stackrel{?}{\geq} 21$ $21 \geq 21$ True ; -4 is in the solution set 2. $x = 6 : ([6] - 3)([6] + 1) \stackrel{?}{\geq} 21$ $(3)(7) \stackrel{?}{\geq} 21$ $21 \geq 21$ True ; 6 is in the solution set	
6	Check Intervals: 1. $(-\infty, -4) : \text{Test Point } x = -6 ; ([-6] - 3)([-6] + 1) \stackrel{?}{\geq} 21$ $(-9)(-5) \stackrel{?}{\geq} 21$ $45 \geq 21$ True ; $(-\infty, -4)$ is in the solution set 2. $(-4, 6) : \text{Test Point } x = 0 ; ([0] - 3)([0] + 1) \stackrel{?}{\geq} 21$ $(-3)(1) \stackrel{?}{\geq} 21$ $-3 \geq 21$ False 3. $(6, +\infty) : \text{Test Point } x = 10 ; ([10] - 3)([10] + 1) \stackrel{?}{\geq} 21$ $(7)(11) \stackrel{?}{\geq} 21$ $77 \geq 21$ True ; $(6, +\infty)$ is in the solution set	
7	Solution Set: $(-\infty, -4] \cup [6, +\infty)$	

Graph of the solution set:

